Elasticity of single-crystal periclase at high pressure and temperature: The effect of iron on the elasticity and seismic parameters of ferropericlase in the lower mantle

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ABSTRACT

In this study, we measured the sound velocities of single-crystal periclase by Brillouin light scattering (BLS) combined with in situ synchrotron X-ray diffraction (XRD) up to ~30 GPa and 900 K in an externally heated diamond-anvil cell (EHDAC). Our experimental results were used to evaluate the combined effects of pressure and temperature on the elastic moduli of single-crystal periclase using third-order Eulerian finite-strain equations. All of the elastic moduli increased with increasing pressure but decreased with increasing temperature, except the off-diagonal modulus C_{12}, which remained almost constant up to ~30 GPa and 900 K. The derived aggregate adiabatic bulk and shear moduli (K_s, G_s) at ambient conditions were 162.8(±0.2) and 130.3(±0.2) GPa, respectively, consistent with literature results. The pressure derivatives of the bulk [∂K_s/∂P] and shear moduli [∂G_s/∂P] at ambient conditions were 3.94(±0.05) and 2.17(±0.02), respectively, whereas the temperature derivatives of these moduli [∂K_s/∂T] and [∂G_s/∂T] at ambient conditions were ~0.025(±0.001) and ~0.020(±0.001) GPa/K, respectively. A comparison of our experimental results with the high-pressure (P) and high-temperature (T) elastic moduli of ferropericlase (Fp) in the literature showed that all the elastic moduli of Fp were linearly correlated with the FeO content up to approximately 20 mol%. These results allowed us to build a comprehensive thermoelastic model for Fp to evaluate the effect of Fe-Mg substitution on the elasticity and seismic parameters of Fp at the relevant P-T conditions of the lower mantle. Our modeling results showed that both the increase of the Fe content in Fp and the increasing depth could change the compressional wave anisotropy (AVP) and shear wave splitting anisotropy (AVS) of Fp in the upper parts of the lower mantle. Furthermore, using our modeling results here, we also evaluated the contribution of Fp to seismic lateral heterogeneities of thermal or chemical origin in the lower mantle. Both the thermally induced and Fe-induced heterogeneities ratios (R_{SP} = ∂lnV_P/∂lnV_S) of Fp from 670 to 1250 km along a representative lower mantle geotherm increased by ~2–5% and ~15%, respectively. The thermally induced R_{SP} value of Fp20 is ~30% higher than Fp10, indicating that the Fe content has a significant effect on the thermally induced R_{SP} of Fp. Compared to the seismic observation results (R_{SP} = 1.7–2.0) in the upper regions of the lower mantle, the Fe-induced R_{SP} value of Fp is more compatible than the thermally induced R_{SP} value of Fp20 (the expected composition of Fp in the lower mantle) within their uncertainties. Thus, we propose that Fe-induced lateral heterogeneities can significantly contribute to the observed seismic lateral heterogeneities in the Earth’s lower mantle (670–1250 km).

Keywords: Elasticity, periclase, Brillouin light scattering, lower mantle, diamond anvil cell

INTRODUCTION

Periclase (MgO) is a classic, simple oxide that crystallizes in the rock-salt structure with no known experimental phase transition up to 250 GPa at least (e.g., Dorfman et al. 2012; Duffy et al. 1995a; McWilliams et al. 2012). The rock-salt structured MgO also represents one of the most common yet simply structured materials in the deep Earth. The structure can potentially be stable up to approximately 400 GPa based on computational studies and laser shock experiments (e.g., Karki et al. 1997; Belonoshko et al. 2010; McWilliams et al. 2012; Coppari et al. 2013; Oganov et al. 2003). MgO also has very high melting temperatures compared to other mantle minerals (e.g., Zerr and Boehler 1994; Ito et al. 2004; McWilliams et al. 2012; Tateno et al. 2014; Kimura et al. 2017). The wide P-T stability of MgO covers relevant high P-T conditions of the deep earth (Duffy and Ahrens 1995) and possibly terrestrial planets or exoplanets (Coppri et al. 2013; Duffy et al. 2015; Bolis et al. 2016). Therefore, precise knowledge of the elastic properties of MgO under high P-T conditions is crucial for constructing a reliable mineralogical model of the Earth’s lower mantle. There have been an increasing number of studies on the elastic behavior of MgO covering a range of high-pressure or high-temperature conditions using different techniques, including static XRD (e.g., Utsumi et al. 1998; Fei 1999; Dewaele et al. 2000; Speziale et al. 2010; McWilliams et al. 2012; Tateno et al. 2014; Kimura et al. 2017).
al. 2001; Jacobsen et al. 2008), BLS (e.g., Sinogeikin and Bass 2000; Zha et al. 2000; Murakami et al. 2009, 2012), ultrasonic interferometry (e.g., Yoneda 1990; Chen et al. 1998; Reichmann et al. 1998; Li et al. 2006), shockwave compressions (e.g., Duffy and Ahrens 1995; Coppari et al. 2013), as well as theoretical studies (e.g., Isaak et al. 1990; Karki et al. 1999; Matsui et al. 2000; Wu et al. 2008; Dorogokupets 2010). To date, however, the elasticity of single-crystal MgO at simultaneous high P-T conditions is limited to 8 GPa and 1600 K (Chen et al. 1998), much lower than the P-T conditions expected in the lower mantle, which extends at depths corresponding to pressures above 23 GPa.

MgO forms a solid solution with FeO, and in a MgO-rich composition, it is known as ferropericlase (Fp) (Mg,Fe)O while magnesiowustite is named for a FeO-rich composition. In the Earth’s lower mantle, Fp is believed to be the second most abundant mineral, coexisting with the most abundant (Al,Fe)-bearing bridgmanite (Bgm) and Ca-perovskite (e.g., Ringwood 1975; Kung et al. 2002; Lin et al. 2005, 2006; Marquardt et al. 2009a, 2009b). Experiments on iron partitioning between Fp and Bgm [Kp = (Fe/Mg)Fp/(Fe/Mg)Bgm] at high P-T conditions suggest that the FeO content in Fp lies in the range of 10–20 mol% for potential compositional models of the lower mantle (e.g., Mao et al. 1997; Wood 2000; Andraut 2001; Irfune et al. 2010). The influences of Fe-Mg substitution on the physical properties of Fp, especially across its electronic spin transition, have recently attracted significant interest to further our understanding of seismic observations and the geodynamical processes of the lower mantle (e.g., Lin et al. 2006, 2013; Fei et al. 2007; Crowhurst et al. 2008; Marquardt et al. 2009; Wu and Wentzcovitch 2014; Muir and Brodholt 2015; Yang et al. 2015). The effect of Fe-Mg substitution on the elastic properties of Fp has been investigated for the whole MgO-FeO system (e.g., Jacobsen et al. 2002; Muir and Brodholt 2015). In particular, previous studies on the effect of FeO in Fp showed that the substitution of FeO strongly increased the density and reduced the velocities of Fp (e.g., Badro et al. 2003; Tsuchiya et al. 2006; Lin et al. 2013; Muir and Brodholt 2015; Yang et al. 2015). However, the fundamental question of how FeO substitution affects the elastic moduli of Fp at high P-T conditions still needs to be better addressed experimentally.

Recently, there have been several studies attempting to characterize the effects of FeO on the full elasticity of Fp at the high P or high P-T conditions of the lower mantle (e.g., Jacobsen et al. 2002; Jackson et al. 2006; Reichmann et al. 2008; Marquardt et al. 2009a; Yang et al. 2015, 2016). Single-crystal XRD and ultrasonic interferometry measurements of the full elastic moduli for a wide range of compositions in the MgO-FeO system at ambient conditions have been documented (Jacobsen et al. 2002). In situ ultrasonic interferometry together with synchrotron XRD measurements on polycrystalline MgO have also been conducted up to 23.6 GPa and 1650 K, and used to establish an independent absolute pressure scale at high P-T conditions (Li et al. 2006; Tange et al. 2009; Kono et al. 2010). However, ultrasonic technique measurements are limited in pressure (<30 GPa) and are most readily performed on polycrystalline samples (e.g., Kung et al. 2002; Li et al. 2005, 2006; Li and Zhang 2005), thus, they only provide limited information on the elastic properties of minerals. Nowadays, BLS coupled with diamond-anvil cells (DAC) is the most commonly used technique to measure the single-crystal elasticity of mantle minerals (e.g., Duffy et al. 1995b; Sinogeikin and Bass 2002; Sang and Bass 2014; Yang et al. 2014; Wu et al. 2016; Fu et al. 2017). It has tremendous advantages at extremely high P-T conditions for optically transparent and translucent samples (e.g., Marquardt et al. 2009a; Yang et al. 2015) and to derive the complete elastic moduli of single-crystal materials (Speziale et al. 2014). BLS has been used to study the single-crystal elasticity of MgO at pressures up to 50 GPa at room temperature (Zha et al. 2000) and temperatures up to 2500 K at room pressure (Sinogeikin et al. 2000, 2004a). Simultaneous high P-T single-crystal elasticity studies of the candidate minerals (e.g., olivine, pyroxene, garnet, spinel, ringwoodite, and Fp) of the Earth’s interior were also reported up to 50 GPa and 1300 K using the BLS technique (e.g., Mao et al. 2012, 2015; Lu et al. 2013; Yang et al. 2014, 2016; Zhang and Bass 2016; Duan et al. 2018). For the single-crystal elasticity of Fp, BLS coupled with an EHDAC was reported up to 50 GPa and 900 K (Yang et al. 2016), while the high-pressure single-crystal elasticity of Fp was reported up to 96 GPa at room temperature (Marquardt et al. 2009a; Yang et al. 2015). However, studying the single-crystal elasticity of Fp with more than 10 mol% FeO (hereafter written as Fp10) is difficult because Fp with a higher amount of FeO is known to be too optically dark to perform the BLS measurement. Using high-pressure inelastic X-ray scattering (IXS) measurements (Fiquet et al. 2004) of the acoustic phonon dispersions of Fp to derive the full elastic moduli could be a solution to these problems. However, the reported elastic moduli of Fp17 in high-pressure IXS measurements (Antonacci et al. 2011) have been inconsistent with other experimental results (impulsive stimulated light scattering, and BLS) (e.g., Crowhurst et al. 2008; Marquardt et al. 2009a, 2009b) and theoretical predictions (e.g., Wentzcovitch et al. 2009; Wu et al. 2009). Thus, the reliability of the IXS experimental results has been questioned because the IXS technique is not a direct method to obtain velocities but uses the acoustic phonon dispersions at very high frequencies to extract the velocities (Fiquet et al. 2004), which rises to an inevitable bias in the velocities. Insofar, there is a lack of comprehensive knowledge on the elasticity of MgO and Fp at the relevant high P-T conditions of the lower mantle.

In this study, we simultaneously measured the acoustic wave velocities and density of single-crystal MgO at high P-T conditions up to ~30 GPa and 900 K using in situ BLS and XRD in an EHDAC. These results were then used to evaluate the high P-T effects on the sound velocities and elastic moduli of MgO. Using the obtained elastic moduli of MgO at high P-T conditions as an end-member reference, together with the elastic moduli of Fp from previous BLS studies, we built a comprehensive thermoelastic model of Fp with up to 20 mol% FeO at the high P-T conditions relevant to lower mantle. We also used these results to evaluate the effects of FeO substitution on the elasticity of Fp, including the acoustic wave velocity anisotropies and seismic parameters. Finally, we used our results to interpret the seismic anisotropy and heterogeneities of the Earth’s lower mantle.

**Experimental methods**

A single-crystal MgO platelet of 10 × 10 mm square and 0.5 mm thick with (100) crystallographic orientation was purchased from MTI Corporation, which was grown by an arc melting method and natural cooling. The crystal platelet was >99.95% pure with no visible inclusions or microcracking. The X-ray rocking curve of the platelet showed an orientation of <100> [0.2°] on the crystal surface.
Analysis of the XRD patterns of the crystal showed a cubic rock-salt structure with a lattice parameter ($a$) of 4.2163(2) Å and a density ($\rho$) of 3.58(1) g/cm$^3$ at ambient conditions.

To prepare our high $P$-$T$ BLS and XRD experiments in an EHDAC, the platelet was polished down on both sides to approximately 20–30 μm thick in the (100) crystallographic orientation using 3M diamond lapping films with an average grain size of 0.3 μm. The thin polished platelet was then cleaved into several ~70 × 70 μm pieces. Round Re disks of 250 μm thick and 3 mm in diameter were pre-indentated to 50–60 μm thick using a pair of diamond anvils with 500 μm culets. Subsequently, a cylindrical 250 μm diameter hole was drilled in the pre-indentated area and used as the sample chamber. An R-type thermocouple was used for the high-temperature measurements of the sample chamber in the EHDAC (Sino-geikin et al. 2006; Kantor et al. 2012; Yang et al. 2014, 2016; Mao et al. 2015). The thermocouple was attached to one of the diamond surfaces approximately 500 μm away from its culet and cladded with a ceramic adhesive (Resbond 920), which was thermally conductive and electrically insulating. The EHDAC was also equipped with an alumina ceramic holder that was coiled with two Pt wire strings; each was 200 μm diameter and 48 cm in length (Lu et al. 2013; Mao et al. 2015; Yang et al. 2016). The Pt wire heater had a resistance of approximately 1 Ω at ambient conditions. A single-crystal platelet was then placed into the sample chamber, together with gold (Au) powder as the pressure calibrant for the XRD experiments (Fei et al. 2007) as well as a few ruby spheres as pressure indicators for the neon gas-loading (Mao et al. 1986) (Fig. 1a). The neon pressure medium was loaded into the sample chamber using the gas loading system in the Mineral Physics Laboratory of the University of Texas in Austin (Lu et al. 2013; Mao et al. 2015; Yang et al. 2016).

We conducted the high $P$-$T$ BLS combined with XRD measurements at beamline 13-BMD of the GeoSoilEnviرو Consortium for the Advanced Radiation Sources (GSECARS) of the Advanced Photon Source (APS), Argonne National Laboratory (ANL). An incident X-ray beam of 0.3344 Å wavelength focused to 7 × 20 μm$^2$ diameter (Sino-geikin et al. 2006) was used to confirm the platelet orientation and to determine the unit-cell volume of the crystal in the EHDACs. To avoid oxidation and failure of the diamond anvils and Pt wires at high temperature, the EHDAC was mounted inside a water-cooled holder with 150 μm thick silica glass windows, and Ar with 2% H$_2$ gas mixture continuously flowed through the EHDAC during heating (Sino-geikin et al. 2006). To minimize pressure instability for each given heating run, the sample chamber was heated to a given temperature and then stabilized for at least 30 min, and its pressure was continuously monitored using XRD until the pressure was sufficiently stable for the BLS experiments. The pressure was determined from the measured lattice parameters of Au at high $P$-$T$ using the third-order Birch-Murnaghan equation of state of Au (Fei et al. 2007), and the temperature of the sample chamber was from the thermocouple measurements. BLS measurements were only conducted when no significant change in pressure was confirmed by the analysis of the XRD patterns of the Au calibrant. To ensure the pressure stability of the experiments a series of XRD patterns of the Au pressure calibrant were collected before and after the BLS measurements of pressure determinations at high $P$-$T$. The pressure uncertainties were determined using multiple measurements from the pressures before and after the BLS measurements for each $P$-$T$ point. Temperatures of the sample chamber were actively stabilized within ±1 K using the temperature-power feedback program with a remotely controlled Tektronix Keithley DC power supply during the experiments (Sino-geikin et al. 2006). The uncertainties of the unit-cell parameters of MgO were typically in the order of 0.03% (Supplemental Table S1), indicating that the MgO sample remained sufficiently high quality for the XRD and BLS experiments at high $P$-$T$ conditions. Analysis of the XRD pattern of the sample was used to determine the density of MgO at each $P$-$T$ condition before and after the BLS measurements.

The single-crystal XRD patterns (Fig. 1b) were also taken to verify the [100] crystallographic direction of the MgO platelet before carrying out the BLS measurements. Then, the motorized DAC rotation stage, which was perpendicular to the focused X-ray beam, was rotated by 45° to get the [110] crystallographic direction of the MgO platelet. Analysis of the XRD spots of the MgO crystal showed a high-quality single-crystal nature with a typical full-width at half maximum (FWHM) of a diffraction peak at ±0.2° (Fig. 1b). High $P$-$T$ BLS spectra of the single-crystal MgO along the [100] and [110] crystallographic directions as well as XRD spectra were collected up to ~30 GPa at selected temperatures of 300, 500, 700, and 900 K (Figs. 2 and 3, and Supplemental Table S1). The Brillouin system was equipped with a Coherent Verdi V2 solid-state laser with a wavelength of 532 nm, and a laser head power of 0.4 W was used for the BLS measurements. BLS spectra were collected in the symmetric forward scattering geometry with an external scattering angle of 50° using a six-pass Sandercoc-type piezoelectrically scanning tandem Fabry-Pérot interferometer (Sandercoc 1982). The interferometer was equipped with a Perkin Elmer MP983 photo counting module with a low dark count rate of ~2 counts/s at room temperature (Sino-geikin et al. 2006). The laser beam focused on the sample position was approximately 15 μm in diameter. The external scattering angle of the system was calibrated using silicate glass and distilled water standards (Ostwald et al. 1977; Polian et al. 2002). The acoustic $V_p$ and $V_S$ velocities of the sample were derived from the analysis of the measured Brillouin frequency shift as follows:

\[ V_{S_0} = (\lambda_s \lambda_{0s}) \frac{2 \sin(\theta/2)}{\lambda_0} \]  

where $V_{S_0}$ is the acoustic compressional or shear wave velocity, respectively, $\lambda_s$ is the incident laser wavelength of 532 nm, $\lambda_{0s}$ is the Brillouin frequency shift, and $\theta$ is the external scattering angle of 50°.

**Figure 1.** Representative sample chamber image and X-ray diffraction image along the principal crystallographic axis [100] of single-crystal MgO platelet at high $P$-$T$ conditions. (a) MgO (100) platelet, together with Au and a ruby sphere calibrant, in Ne medium. (b) Representative X-ray diffraction pattern along the principal crystallographic axis [100] of single-crystal MgO platelet at 11.65 GPa and 700 K. The inset shows the high-quality single-crystal nature with a typical FWHM of a diffraction peak of MgO at ±0.2°. (Color online.)
Results

Our collected BLS spectra along the [100] and [110] crystallographic directions showed strong $V_p$ and $V_S$ peaks with high signal-to-noise ratios at high $P$-$T$ conditions (Fig. 2). Although two polarized $V_p$ peaks were expected to exist, only one $V_S$ peak was observed in our study. This is a result of the polarization of the $V_S$ in the (100) crystallographic orientation of the MgO crystal interacting with the incident laser. Brillouin signals of the neon pressure medium were also observed at pressures below ~8 GPa, but they were too weak to be visible in the BLS spectra when the pressure was increased above approximately 8 GPa (Fig. 2). Analysis of the $V_p$ and $V_S$ velocities of MgO as a function of pressure at each given temperature showed that the $V_p$ along the [100] and [110] directions as well as $V_S$ along the [110] direction (hereafter written as $V_S[110]$, $V_S[100]$, and $V_S[110]$, accordingly) increased with increasing pressure and decreased with increasing temperature. However, $V_S$ along the [100] (hereafter written as $V_S[100]$) remained almost unaffected by increasing $P$-$T$ up to ~30 GPa and 900 K (Fig. 4). These observations indicate strong $P$-$T$ effects on the $V_S$ anisotropy.

The elastic tensors of cubic MgO can be fully described by three independent elastic moduli, $C_{11}$, $C_{12}$, and $C_{44}$. The use of the (100) platelets in this study permits determination of the elastic moduli ($C_{11}$, $C_{12}$, $C_{44}$) using the velocity determined in the [100] and [110] directions (Fig. 5), respectively, together with the measured density (Supplemental Table S2). The equations used in the analysis were derived from Christoffel’s equation (Grimsditch 2001):

\[ \rho V_p^2[100] = C_{11} \] (2)
\[ \rho V_p^2[110] = C_{11} + 2C_{44} + C_{12} \] (3)
\[ \rho V_S^2[110] = (C_{11} + 2C_{44})/2 \] (4)
\[ \rho V_S^2[100] = (C_{11} - C_{12})/2 \] (5)

where $\rho$ is the density of MgO; $V_p[100]$ and $V_S[100]$ are the measured compressional- and shear-wave velocities of MgO along the [100] direction, respectively; $V_p[110]$ and $V_S[110]$ are the compressional- and shear-wave velocities along the [110] direction, respectively; and $C_{11}$, $C_{12}$, and $C_{44}$ are the compressional, off-diagonal, and shear moduli of MgO, respectively.

We used the least squares regression method utilizing the aforementioned four equations instead of only three equations for the modeling because examination of Equations 2–5 showed that the three elastic moduli ($C_{11}$, $C_{12}$, and $C_{44}$) could be determined more accurately. The uncertainties of the elastic moduli (Supplemental Table S2) were estimated using standard error propagation in these derivations. We should note that these equations were derived from the general Christoffel’s equation (Every 1980):

Figure 2. Representative Brillouin spectra of single-crystal periclase MgO at high pressure and temperature. Open circles = experimental data; solid lines = fitted $V_p$ and $V_S$ peaks, respectively. (Color online.)

Figure 3. Pressure-volume-temperature relations of single-crystal periclase MgO. The results are derived from analysis of X-ray diffraction measurements in EHDACs. Solid symbols represent experimental data at 300, 500, 700, and 900 K. Solid lines are fits to experimental data using the third-order Birch-Murnaghan equation of state. The inset shows the density of MgO as a function of pressure at the given high temperatures. (Color online.)

Figure 4. Acoustic velocities of the single-crystal periclase MgO along the [110] and [100] crystallographic directions as a function of pressure and temperature. Solid circles = experimental data; solid lines = modeled results using the finite-strain theory. (Color online.)
where \( \rho \) is the density from XRD measurements, \( V \) is the measured acoustic velocity, \( \delta_0 \) is the Kronecker \( \delta \), and \( \Gamma_2 \) is the coefficient in the Christoffel matrix. The values of the Christoffel coefficients \( \Gamma_2 \) depend on the single-crystal constants \( C_{ij} \) in the reduced Voigt notation, where the propagation direction of the sound velocity is described by the direction cosines of the acoustic wavevector, \( n \).

Using the derived elastic moduli of MgO, we calculated the aggregate adiabatic bulk and shear moduli \( (K_s, G) \) (Supplementary Table S1 and Figs. 6a and 6b) using the Voigt-Ruess-Hill averages (Hill 1952):

\[
K_s = C_{11} - 2C_{33}/3
\]

\[
G = \left[ (C/5 + 3C_{33}/5) + 5C_{44}C/(4C_{44} + 3C) \right]/2
\]

\[
C = C_{11} - C_{12}.
\]

The derived \( K_{50} \) and \( G \) at ambient conditions were 162.8(\pm0.2) GPa and 130.3(\pm0.2) GPa, respectively. The aggregate velocities of MgO (Figs. 6c and 6d) were calculated using the equations:

\[
V_p = \sqrt{(K_s + 4G/3)/\rho}
\]

\[
V_s = \sqrt{G/\rho}.
\]

The pressure and temperature derivatives of the elastic moduli were obtained by fitting the experimental data using the third-order finite strain equations (Tables 1 and 2) (Birch 1978; Duffy and Anderson 1989):

\[
C_{ij}(T) = (1+2f)^{2/3} [C_{ij}(T) + a_i f] + a_2 P
\]

\[
C_{ij}(T) = C_{ij}(300 \text{ K}) + (T - 300)[(\partial C_{ij}/\partial T)_T - a_2] - 7C_{ij}(T)
\]

\[
f = (1/2)\left( [V_d(T)/V]^{23} - 1 \right)
\]

\[
V_s(T) = V_s(300\text{K}) \exp \int_{300}^{T} \alpha dT
\]

\[
\left( \partial C_{ij}/\partial P \right)_T = \left( \partial C_{ij}/\partial P \right)_{300\text{K}} \exp \int_{300}^{T} \alpha dT.
\]

where \( P \) is the measured pressure; \( C_{ij}(300 \text{ K}) \) is the elastic modulus at ambient conditions; \( C_{ij}(T) \) is the elastic modulus at temperature \( T \) and 1 bar; \( C_{ij}(T) \) is elastic modulus at temperature \( T \) and high pressures; \( (\partial C_{ij}/\partial T)_T \) is the temperature derivative of the elastic modulus at constant \( P \) and ambient \( T \); \( (\partial C_{ij}/\partial P)_T \) is the pressure derivative of the elastic modulus at constant \( T \) and ambient \( P \); \( (\partial C_{ij}/\partial P)_{300\text{K}} \) is the pressure derivative of the elastic modulus at ambient conditions; \( a_2 \) is the thermal expansion coefficient at ambient conditions. \( K_{50}(T) \) is the isothermal bulk modulus at temperature \( T \) and 1 bar, and can be calculated as:

\[
K_{50}(T) = K_{50}(300 \text{ K}) + (\partial K_{50}/\partial T)_T (T - 300)
\]

\[
K_{50}(300 \text{ K}) = K_{50}(300 \text{ K})/(1 + \alpha T \times 300)
\]

\[
(\partial K_{50}/\partial T)_T = (\partial K_{50}/\partial T)_T (1 + \alpha T) - K_{50}(T)(1 + \alpha T)^2 \frac{\alpha T \times (\partial T/\partial \alpha)}{(\partial T/\partial \alpha)}
\]

where \( \alpha \) is the thermal expansion coefficient at ambient conditions, and \( \gamma \) is the Grüneisen parameter at ambient conditions with

**Figure 5.** Single-crystal elastic moduli of periclase MgO as a function of pressure and temperature. Solid lines are the fitted results using the third-order finite-strain equation. (Color online.)

**Figure 6.** Aggregate elastic moduli and velocities of periclase MgO as a function of pressure and temperature. Solid lines are fits to the experimental data using the third-order finite-strain equation. (Color online.)
a literature value of 1.442 (Tange et al. 2009). The temperature derivative of $K_b$, $(\partial K_b/\partial T)_b$, and the pressure derivative of $K_b$, $(\partial K_b/\partial P)_b$, were derived by fitting $K_b$ at high $P$-$T$ using the third-order finite strain equations (Tables 1 and 2):

\[ K_b = K_{bs}(1 + 2f^2)[1 + 3(\partial K_b/\partial T)_b - 5f] \]  
\[ K_{ss} = K_{ss}(300 \text{ K}) + (\partial K_b/\partial T)_b(T - 300) \]  
\[ (\partial K_b/\partial P)_b = (\partial K_b/\partial P)_{300 \text{ K}} \exp \int_{300}^{T} dT \]  

where $K_{ss}(300 \text{ K})$ is the adiabatic bulk modulus at ambient conditions, $K_{ss}(T)$ is the adiabatic bulk modulus at temperature $T$ and 1 bar, $K_{st}(T)$ is the adiabatic bulk modulus at temperature $T$ and high pressures, and $(\partial K_b/\partial P)_{300 \text{ K}}$ is the pressure derivative of $K_b$ at ambient conditions. We also constrained the pressure and temperature derivatives of the shear modulus $G$ of MgO using the third-order finite strain equations:

\[ G(T) = (1 + 2f^2)[G_b(T) + b_f f] \]  
\[ G_b(T) = \frac{G_b(300 \text{ K}) + (\partial G_b/\partial T)_b(T - 300)}{b_i} = 3K_{ss}(T)(\partial G_b/\partial P)_b - 5G_b(T) \]  
\[ (\partial G/\partial P)_b = (\partial G/\partial P)_{300 \text{ K}} \exp \int_{300}^{T} dT \]  

where $G_b(300 \text{ K})$ is the shear modulus at ambient conditions; $G_b(T)$ is the shear modulus at temperature $T$ and 1 bar; $G(T)$ is the shear modulus at temperature $T$ and high pressures; $(\partial G/\partial P)_b$ and $(\partial G/\partial T)_b$ are the pressure and temperature derivatives of the shear modulus, respectively, and $(\partial G/\partial P)_{300 \text{ K}}$ is the pressure derivative of the shear modulus at ambient conditions (Tables 1–2).

**DISCUSSION**

The single-crystal elasticity of MgO at high $P$-$T$

By combining the BLS and single-crystal XRD measurements, we derived the full single-crystal elasticity of MgO at simultaneously high $P$-$T$ conditions, including all of the elastic moduli ($C_{ij}$ values, $C_{ij}$, and G) (Figs. 5 and 6, Supplemental Table S1 and S2). All $C_{ij}$ values and $K_b$ exhibit a linear increase with pressure at the given temperatures (Figs. 5 and 6a), whereas $G$ shows a slight pressure-dependent concave curvature (Fig. 6b). Compared with the values from ultrasonic interferometry and BLS experiments, the derived pressure derivatives for the compressional moduli $C_{11s}$, off-diagonal moduli $C_{12s}$, and bulk modulus $K_b$ at ambient conditions in this study are slightly lower than the corresponding values in the literature (Jackson and Niesler 1982; Yoneda 1990; Sinogeikin and Bass 2000; Li et al. 2006; Kono et al. 2010), except the pressure derivative of $C_{11s}$, which is consistent with the results in this study. This indicates an enhanced temperature effect on these elastic moduli at high pressures. In addition, the pressure derivatives of the shear moduli ($C_{44}$ and $G$) at ambient conditions are indistinguishable from the values in previous studies within experimental uncertainties (Tables 1 and 2), except a larger pressure derivative of $G$ at ambient conditions was reported by Zha.
Compressional wave velocity and shear wave splitting anisotropy of MgO

The elastic wave anisotropy of minerals expresses the difference in stiffness of a structure in different crystallographic directions, and shear wave anisotropy can be an indicator of the stability of minerals (Sinogeikin and Bass 2000). Knowledge of the velocity anisotropy of minerals at high P-T conditions may help to explain the seismic anisotropy within the Earth’s interior (Long and Becker 2010; Mainprice 2015). To understand the evolution of the velocity anisotropy of MgO at high P-T conditions, the \( V_P \) and \( V_S \) velocities at different propagation directions and anisotropy distributions were calculated using our derived \( C_{ij} \) values and density at each given P-T point (Mainprice 1990; Mainprice et al. 2000). The percentage anisotropy for \( V_P (AV_P) \) is defined here as:

\[
AV_P = \left( \frac{V_{P_{\text{max}}} - V_{P_{\text{min}}}}{V_{P_{\text{max}}} + V_{P_{\text{min}}}} \right) \times 200\% \tag{28}
\]

where \( V_{P_{\text{max}}} \) and \( V_{P_{\text{min}}} \) represent the maximum and minimum \( V_P \) velocities, respectively. The polarization anisotropy factor of \( V_S (AV_S) \), also called the shear wave splitting factor, is the anisotropy percentage of the two \( V_S \) in a given direction and is defined as:

\[
AV_S = \left( \frac{V_{S_{\text{max}}} - V_{S_{\text{min}}}}{V_{S_{\text{max}}} + V_{S_{\text{min}}}} \right) \times 100\% \tag{29}
\]

where \( V_{S_{\text{max}}} \) and \( V_{S_{\text{min}}} \) are the two orthogonally polarized \( V_S \) velocities in the given propagation direction, and \( V_S \) represents the aggregate shear wave velocity. A contoured upper hemisphere stereogram of \( V_P \) and \( V_S \) for MgO at two representative P-T conditions from our experiments is shown in Figure 7. These results show that, even though MgO is highly anisotropic at ambient conditions, with an \( AV_P \) of 11.0% and \( AV_S \) of 21.5% (Fan et al. 2015; Mainprice 2015), \( AV_P \) reduces to 7.1% and \( AV_S \) to 14.1% at 7.17 GPa and 500 K in this study (Fig. 7). \( V_P \) and \( V_S \) decrease to 0.5 and 1.2%, respectively, at the maximum P-T conditions of 29.63 GPa and 900 K in our experiments, showing that MgO is almost elastically isotropic at such high P-T conditions (Fig. 7). These results clearly show that high P-T have a significant impact on the elastic wave velocity anisotropy of MgO.

Modeling the elasticity of (Mg,Fe)O ferropericlase at high P-T conditions

MgO is an end-member of (Mg,Fe)O ferropericlase, the second most abundant mineral in the lower mantle. Since the (Mg,Fe)O solid solution system crystallizes in the rock-salt structure at relevant lower-mantle P-T conditions, it is possible to use our MgO results as an end-member reference for understanding the elasticity of the (Mg,Fe)O system at high P-T conditions. To model the elasticity of Fp with different FeO contents at high P-T conditions, we initially compared our MgO results to literature elasticity values of Fp (Fp1, Fp6, and Fp10) derived from Brillouin measurements (Reichmann et al. 2008; Marquardt et al. 2009a; Yang et al. 2016) (Figs. 8 and 9). Considering the limited available single-crystal elastic moduli results of Fp from other methods (Jacobsen et al. 2002; Crowhurst et al. 2008; Antonangeli et al. 2011), and avoiding the potential systematic errors in different experimental methods (for example, incompatible results by IXS methods with other available studies; the possible effect on the pressure derivatives of elastic moduli by ultrasonic methods vs. Brillouin scattering), we only used literature Brillouin results in our modeling. We also limited the modeling to Fp with up to 20 mol% FeO because of the limited Fp compositions in the literature (Reichmann et al. 2008; Marquardt et al. 2009a; Yang et al. 2016) and the relevant Fp composition of approximately Fp20 in the Earth’s lower mantle (Ringwood 1975; Mao et al. 1997; Wood 2000; Andraut 2001; Irifune et al. 2010).

Our analysis of the single-crystal elastic moduli (\( C_{ij} \)) of MgO as a function of the FeO content in mol% at ambient conditions showed that the substitution of FeO in Fp had a positive effect on \( C_{12} \) and a negative effect on \( C_{11} \) and \( C_{44} \). Within experimental uncertainties, \( C_{12} \) linearly increased with FeO content, while \( C_{11} \) and \( C_{44} \) decreased linearly with increasing FeO content (Fig. 8):

\[
\begin{align*}
C_{11} &= 296.8(\pm 1.8) - 184.5(\pm 30.4)X\text{Fe} \tag{30} \\
C_{12} &= 95.6(\pm 0.7) + 71.3(\pm 12.6)X\text{Fe} \tag{31} \\
C_{44} &= 152.7(\pm 0.2) - 108.4(\pm 2.9)X\text{Fe} \tag{32}
\end{align*}
\]

where \( X\text{Fe} = \frac{M_{\text{FeO}}}{M_{\text{FeO}} + M_{\text{MgO}}} \), \( X\text{Fe} \) is the mole fraction, and \( M_{\text{FeO}} \) and \( M_{\text{MgO}} \) are the molar content. In addition, Jacobsen et al. (2002) reported the effects of FeO substitution on the \( C_{ij} \) values of (Mg,Fe)O using ultrasonic interferometry with high-frequency shear waves at ambient conditions. They fitted their \( C_{ij} \) values of the MgO-FeO system using a second-order or a third-order polynomial. A close inspection of the polynomial fits showed that there was a close linear relationship between the \( C_{ij} \) and FeO content when the FeO content in Fp is less than 20 mol% (as shown by the dashed lines in Fig. 8). Thus, we used the linear relationship between the \( C_{ij} \) and FeO content of Fp at ambient...
We also evaluated the high $P$–$T$ relationship between the $C_{ij}$ and FeO content by comparing the pressure and temperature derivatives of the single-crystal elastic moduli ($C_{ij}$) of MgO ([($\partial C_{ij}/\partial P$)$_{300K}$ and ($\partial C_{ij}/\partial T$)$_{300K}$]) to the literature results of Fp (Fp6 and Fp10) (Marquardt et al. 2009a; Yang et al. 2016). Analysis of these results showed that within experimental uncertainties, ($\partial C_{ij}/\partial P$)$_{300K}$ and ($\partial C_{ij}/\partial T$)$_{300K}$ increased linearly with increasing FeO content, but ($\partial C_{ij}/\partial P$)$_{300K}$ decreased linearly with increasing FeO content (Fig. 9a):

$$\frac{\partial C_{ij}}{\partial P} = 8.43(\pm 0.13) + 2.68(\pm 1.89)X_{Fe} \quad (33)$$

$$\frac{\partial C_{ij}}{\partial T} = 1.46(\pm 0.09) + 2.00(\pm 1.22)X_{Fe} \quad (34)$$

$$\frac{\partial C_{ij}}{\partial T} = 1.25(\pm 0.01) - 4.31(\pm 0.09)X_{Fe}. \quad (35)$$

Since the experimental temperature derivatives of $C_{ij}$ ($\partial C_{ij}/\partial T$)$_{300}$ of Fp were only available for Fp6 (Yang et al. 2016), we calculated the ($\partial C_{ij}/\partial T$)$_{300}$ of Fp10 using the $C_{ij}$ values at ambient conditions obtained by Marquardt et al. (2009a) and $C_{ij}$ values at high temperatures up to 4000 K obtained by Muir and Brodholt (2015). The results above were then used to estimate the effect of FeO on the ($\partial C_{ij}/\partial T$)$_{300}$ of Fp. Within uncertainties, these results showed that ($\partial C_{ij}/\partial T$)$_{300}$ increased with increasing FeO content, while ($\partial C_{ij}/\partial T$)$_{300}$ decreased with increasing FeO content. Therefore, we fitted the data with a linear relationship between the ($\partial C_{ij}/\partial T$)$_{300}$ and FeO content in Fp (Fig. 9b):

$$\frac{\partial C_{ij}}{\partial T} = -0.063(\pm 0.003) + 0.11(\pm 0.03)X_{Fe} \quad (36)$$

$$\frac{\partial C_{ij}}{\partial T} = 0.0010(\pm 0.0006) + 0.08(\pm 0.01)X_{Fe} \quad (37)$$

$$\frac{\partial C_{ij}}{\partial T} = -0.01(\pm 0.001) - 0.10(\pm 0.02)X_{Fe}. \quad (38)$$

These derived linear relationships for the elastic moduli and their $P$–$T$ derivatives were then combined with finite-strain theory equations (Eqs. 7–23) to evaluate the full elasticity of Fp at high $P$–$T$ conditions. We should emphasize that these linear equations can only be used within the solid solution range of approximately 0–20 mol% FeO. Evaluation of the relationship between the elastic moduli and a higher FeO content at high $P$–$T$ conditions in the (Mg,Fe)O system will require further experimental data in the future.

**FIGURE 7.** Upper hemisphere pole figures of $V_p$ anisotropy and $V_S$ splitting anisotropy of single-crystal perovskite MgO at representative pressures and temperatures. Calculations were performed using the petrophysical software UnicefCareware of Mainprice (1990) with the derived single-crystal elastic moduli from this study. (Color online.)
FeO effects on the velocity profiles of Fp in the Earth’s lower mantle

The Earth’s mantle is generally believed to have a pyrolitic composition (Ringwood 1975). Based on the pyrolite model, Earth’s lower mantle consists of approximately 75 vol% Bgm, 20 vol% Fp, and 5 vol% Ca-silicate perovskite (Ca-Pv) (Ringwood 1975; Irifune 1994; Ricolleau et al. 2009; Irifune et al. 2010). Although the exact composition of Earth’s lower mantle has yet to be unambiguously determined, the current consensus is that Fp contains approximately 20 mol% FeO, while Bgm contains 10 mol% FeO, together with a few percents of Al$_2$O$_3$ in Bgm (e.g., Mattern et al. 2005; Lin and Tsuchiya 2008; Irifune et al. 2010; Lin et al. 2013). The spin transition in both Fp and (Al,Fe)-bearing Mattern et al. 2005; Lin and Tsuchiya 2008; Irifune et al. 2010; Murakami et al. 2007; Murakami et al. 2007), 20 vol% Fp20 (this study), and 5 vol% Ca-Pv (Kudo et al. 2012). The Preliminary Reference Earth Model (PREM) (Dziewonski and Anderson 1981) (Fig. 10). Briefly, the third-order Eulerian finite-strain equations and the third-order Birch-Murnaghan equation of state (Birch 1978) were used to evaluate the $K_s$ and $G$ of the relevant minerals by extrapolating the experimentally derived elastic moduli and their $P$-T derivatives to relevant $P$-T conditions. The reference $P$-$T$ conditions at 670 km deep were ~23.8 GPa and ~1980 K, and the modeling depth was limited to 1250 km (mid-lower mantle) to avoid the complication of the potential effects of the iron electronic spin transition (e.g., see Lin et al. 2013 for a review).

Our modeled velocity profiles showed that substitution of FeO in Fp could significantly reduce both the $V_p$ and $V_S$ velocities at lower mantle conditions; compared to MgO, the $V_p$ and $V_S$ velocities of Fp20 were reduced by ~8% and ~10%, respectively. That is, $(\partial V_p/\partial X_{Fe})$ and $(\partial V_S/\partial X_{Fe})$ are approximately ~0.04 and ~0.03 km/s/kmol, respectively, in the upper part of the lower mantle. Furthermore, the $V_p$ and $V_S$ velocity profiles of Fp20 are ~8% and ~4% lower than the velocity profiles of the PREM, respectively. On the other hand, Bgm10 has the highest $V_p$ profile and MgO has the highest $V_S$ profile among all lower-mantle minerals, while Fp20 has the lowest $V_p$ profile and Ca-Pv has the lowest $V_S$ profile. The depth-dependent velocity profiles of a volume-weighted pyrolitic aggregate for the Earth’s lower mantle, which was obtained from the arithmetic mean aggre-

FIGURE 8. Single-crystal elastic moduli of ferropericlase (Mg,Fe)O as a function of the FeO content at ambient conditions. Solid symbols are experimental Brillouin light scattering results for MgO (this study), Fp1 (Reichmann et al. 2008), Fp6 (Yang et al. 2016), and Fp10 (Marquardt et al. 2009). Solid lines are linear fits to the Brillouin experimental data. Black dashed lines: ultrasonic results at ambient conditions by Jacobsen et al. (2002) for comparison. (Color online.)

FIGURE 9. Pressure and temperature derivatives of the single-crystal elastic moduli of ferropericlase (Mg,Fe)O as a function of the FeO content at high $P$-$T$ conditions. Solid symbols are derived from experimental Brillouin results for MgO (this study), Fp6 (Yang et al. 2016), and Fp10 (Marquardt et al. 2009). Solid lines are linear fits to the Brillouin experimental data. (Color online.)

FIGURE 10. Aggregate $V_p$ and $V_S$ of bridgmanite, ferropericlase, and Ca-perovskite in the Earth’s lower mantle. These results are compared with the PREM model (Dziewonski and Anderson 1981). For the pyrolite mineralogical model, we used 75 vol% Bgm10 (Chantel et al. 2012; Murakami et al. 2007), 20 vol% Fp20 (this study), and 5 vol% Ca-Pv (Kudo et al. 2012). Red line = Fp20; magenta line = Fp10; cyan line = MgO; blue line = Bgm10; green line = Ca-Pv; and crosses = PREM. Error bars represent the propagated uncertainties (±1σ). (Color online.)
Imagery of the compositions (75 vol% Bgm10, 20 vol% Fp20, and 5 vol% Ca-Pv) (Ringwood 1975; Irfune et al. 2010), were extremely consistent with velocity profiles of the PREM within uncertainties.

**Implications**

Seismic wave anisotropy of Fp in the Earth’s lower mantle

Seismic studies of the Earth’s mantle have reported seismic anisotropy that could result from the crystallographic lattice preferred orientation (CPO) of the constituent minerals with velocity anisotropy (Blackman and Kendall 2002; Nippress et al. 2004; Niu and Perez 2004; Karato et al. 2008; Marquardt et al. 2009b; Marquardt and Morales 2012; Walpole et al. 2017). The CPO of the constituent minerals could develop due to mantle convection (Karato 1998; Tackley 2000; Long and Becker 2010; Boneh and Skemer 2014; Mainprice 2015). Therefore, understanding the seismic anisotropy of the Earth’s lower mantle can greatly help us understand the geodynamics of the deep Earth (Mainprice et al. 2000; Long and Becker 2010; Romanowicz and Wenk 2017).

Specifically, the viscosity of Fp seems to be pressure-dependent (Marquardt and Miyagi 2015), but Fp is still among the weakest rheological phases in the lower mantle and can significantly contribute to the seismic anisotropy of the lower mantle (e.g., Marquardt et al. 2009b; Miyagi and Wenk 2016; Immoo et al. 2018). The elastic anisotropy of Fp combined with its rheological weakness can play a significant role in the interpretation of the observed seismic anisotropy in the lower mantle (e.g., Yamazaki and Karato 2001; Yamazaki et al. 2009; Marquardt and Miyagi 2015; Girard et al. 2016).

To decipher the potential influence of Fp on the lower-mantle seismic anisotropy, we calculated the AVp and AVs of Fp10 and Fp20 along a representative geotherm using the aforementioned thermoelastic modeling method (Fig. 11). At a 670 km depth, the AVp and AVs of Fp20 are 3.7% and 8.6%, respectively, and the difference between the vertically VSV and horizontally VSH polarized shear waves is 0.45 km/s. The AVp and AVs of Fp10 are 4.4% and 9.87%, respectively, and the difference between the orthogonally polarized shear waves VSV and VSH is 0.55 km/s. However, at a depth of ~1250 km, the AVp is 5.0%, AVs is 11.42% for Fp20, and the difference between VSH and VSV is 0.66 km/s. The AVp is 3.7% and AVs is 8.09% for Fp10, and the difference between VSH and VSV is 0.51 km/s. These results showed that Fp was clearly SH and VS splitting anisotropy of Fp10 and Fp20 at 670 and 1250 km, respectively. Calculations were performed using the petrophysical software UnicefCareware of Mainprice (1990) with the modeled single-crystal elastic moduli from this study. (Color online.)

Karato and Karki 2001; Li 2009; Wu and Wentzcovitch 2017; Schumacher et al. 2018). However, their interpretation is still uncertain. While some studies have suggested that the seismic heterogeneities of the lower mantle was mainly due to thermal effects (e.g., Forte et al. 1994; Forte 2000; Simmons et al. 2010), many other studies have suggested chemically induced heterogeneities (e.g., Antolik et al. 2003; Resovsky and Trampert 2003; Garnero and McNamara 2008; Kaneshima and Hellfrich 2010; Mosca et al. 2012; Koelmeijer et al. 2016). Distinguishing the thermal or chemical origin of the seismic heterogeneities in the lower mantle is crucial because each origin has a drastically different consequence and affects our understanding of the Earth’s interior dynamic (Karato and Karki 2001). Experimental elasticity studies of the major minerals in the lower mantle (such as Fp) at relevant high P-T conditions play a significant role in understanding the seismic signatures, and also provide a new constraint on the seismic structures and evolution of the lower mantle (Karato and Karki 2001; Yang et al. 2016).

The thermal or chemical origins of the seismic lateral heterogeneities can be constrained by comparing the observed ratios of vari-

**Figure 11.** Upper hemisphere pole figures of the Vp anisotropy and Vs splitting anisotropy of Fp10 and Fp20 at 670 and 1250 km, respectively.
ous seismic parameters with mineral physics results (e.g., Karato and Karki 2001; Wu and Wentzcovitch 2014; Yang et al. 2016). To investigate the thermal variation of the heterogeneities ratios ($R_{SP}$ = $\frac{\partial \ln V/S}{\partial T}$ for Fp), we calculated the thermally induced variations in $V_S$ and $V_P$ for MgO, Fp10, and Fp20 (Fig. 12a). In the modeling, the velocities of these phases were first extrapolated along a representative geotherm (Katsura et al. 2010) based on the derived thermoelastic parameters and finite-strain theory. In addition, we applied a positive and negative temperature perturbation of 200 K to the velocities to determine the $\partial \ln V_S/\partial T$ and $\partial \ln V_P/\partial T$ for Fp. The $R_{SP}$ values of MgO, Fp10, and Fp20 show an increase of ~2–5% from 670 to 1250 km, indicating that high temperature increases the $R_{SP}$ value of Fp. The $R_{SP}$ profile of Fp20~30% and ~50% higher than Fp10 and MgO, respectively. Therefore, our results showed that the thermally induced $R_{SP}$ was sensitive to composition and the FeO content had a significant increasing effect on the thermally induced $R_{SP}$ of Fp in the upper part of the lower mantle. This also agrees with a previous theoretical prediction, which showed that compositional variations could change the thermally induced $R_{SP}$ depth profiles in the lower mantle (Wu and Wentzcovitch 2017).

The amount of FeO in the Earth’s lower mantle minerals is particularly important because it can affect a wide range of elastic properties, including their densities, sound velocities, bulk moduli, and shear moduli (Jacobsen et al. 2002; Yang et al. 2015). Previous studies have also suggested that the variation of FeO content in Fp may be regarded as a potential chemical cause for seismic lateral heterogeneities (van der Hilst and Kárason 1999). Here, we also calculated the Fe-induced variations of $V_S$ and $V_P$ for Fp (MgO, Fp10, and Fp20) from 670 to 1250 km along a representative geotherm (Fig. 12b). Due to change of the Fe content in Fp, the value of $R_{SP}$ shows a distinctly increasing trend from ~1.92 at 670 km to ~2.21 at 1250 km (Fig. 12b), which is similar with the upward trending thermally induced variation of Fp (MgO, Fp10, and Fp20) but has significantly steeper slopes. These results indicate that the value of $R_{SP}$ distinctly increases with increasing Fe content in Fp. Specifically, the value of $R_{SP}$ due to change of the Fe content in Fp is ~10% lower than the thermally induced variation of Fp20. Moreover, our value of $R_{SP}$ due to change of the Fe content in Fp is also ~15% higher than the one from a previous study by Yang et al. (2016) (dot-dashed line in Fig. 12b) within their uncertainties. There are two possible reasons for the slightly different results between this study and Yang et al. (2016). One of them is that we calculated the Fe-induced variations of $V_S$ and $V_P$ for Fp with up to 20 mol% FeO, whereas Yang et al. (2016) only limited Fp with up to 10 mol% FeO. Another reason is that Yang et al. (2016) calculated the relative variations of velocity with a Fe content using the high-pressure and room-temperature elasticity data of MgO (Sinogeikin and Bass 2000) as their benchmark data. These factors clearly highlight the importance of our current simultaneously high P-T elasticity studies of MgO.

In addition, even though some seismic studies showed a decreasing trend of $R_{SP}$ in the upper part of the lower mantle (e.g., Mosca et al. 2012), most seismic studies demonstrated an increasing trend in the same depth region, where the $R_{SP}$ was ~1.7 at the top of the lower mantle and ~2.0 in the mid-lower mantle (e.g., Robertson and Woodhouse 1996; Romanowicz 2001; Simmons et al. 2010). Compared to the seismic observation results (dashed lines in Fig. 12b), the $R_{SP}$ value of the thermally induced variation for Fp10 is consistent with most seismic observations within uncertainty. However, the thermally induced $R_{SP}$ value of Fp20, which is the relevant composition of Fp in the lower mantle, is ~50% higher than most seismic observations within uncertainty for the upper part of the lower mantle (e.g., Robertson and Woodhouse 1996; Romanowicz 2001; Simmons et al. 2010). Thus, based on the results for Fp in this study, we propose that the Fe-induced heterogeneities can offer a significant contribution to the observed seismic lateral heterogeneities in the lower mantle. This also agrees with the results of seismology studies, which showed that the seismic heterogeneities in the lower mantle could not be explained by thermal anomalies alone, and suggested the presence of chemical heterogeneities, might be a local variation of Fe content, as an alternative explanation (e.g., Kellogg et al. 1999; van der Hilst and Kárason 1999; Wysession et al. 1999; Houser et al. 2008). We should note that the above mentioned Fe-induced heterogeneities in the lower mantle did not take the potential contributions from

![Figure 12](https://pubs.geoscienceworld.org/msa/ammin/article-pdf/104/2/262/4627943/am-2019-6656.pdf)

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Bgm into account because Fe preferentially partitions into Fp in the lower mantle (e.g., Auzende et al. 2008; Sakai et al. 2009; Muir and Brodholt 2016; Kaminys and Lin 2017; Xu et al. 2017), and there are few single-crystal elasticity experimental studies of Bgm at high P-T conditions (e.g., Sinogeikin et al. 2004b). Future single-crystal elasticity studies of Fp and Bgm at the relevant P-T and compositional (the possible Fp and Bgm compositions expected in the lower mantle) conditions are needed to provide a more comprehensive understanding of the seismic anisotropy and lateral heterogeneities of the Earth’s lower mantle.

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Kaminsky and Lin (2017); Xu et al. (2017), and there are few single-crystal elasticity experimental studies of Bgm at high P-T conditions (e.g., Sinogeikin et al. 2004b). Future single-crystal elasticity studies of Fp and Bgm at the relevant P-T and compositional (the possible Fe and Bgm compositions expected in the lower mantle) conditions are needed to provide a more comprehensive understanding of the seismic anisotropy and lateral heterogeneities of the Earth’s lower mantle.
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