Layer-Dependent Pressure Effect on the Electronic Structure of 2D Black Phosphorus

Shenyang Huang,^{1,*} Yang Lu⁰,^{2,*,†} Fanjie Wang,¹ Yuchen Lei,¹ Chaoyu Song⁰,¹ Jiasheng Zhang,¹ Qiaoxia Xing,¹

Chong Wang,¹ Yuangang Xie,¹ Lei Mu,¹ Guowei Zhang,³ Hao Yan⁵,⁴ Bin Chen,² and Hugen Yan^{1,5,‡}

¹State Key Laboratory of Surface Physics, Key Laboratory of Micro- and Nano-Photonic Structures (Ministry of Education), and Department of Physics, Fudan University, Shanghai 200433, China

²Center for High Pressure Science & Technology Advanced Research, Shanghai 201203, China

³Institute of Flexible Electronics, Northwestern Polytechnical University, Xi'an 710072, China

⁴CAS Key Laboratory of Experimental Study under Deep-sea Extreme Conditions, Institute of Deep-Sea Science and Engineering,

Chinese Academy of Sciences, Sanya 572000, China

⁵Collaborative Innovation Center of Advanced Microstructures, Nanjing 210093, China

(Received 29 March 2021; accepted 21 September 2021; published 26 October 2021)

Through infrared spectroscopy, we systematically study the pressure effect on electronic structures of few-layer black phosphorus (BP) with layer number ranging from 2 to 13. We reveal that the pressure-induced shift of optical transitions exhibits strong layer dependence. In sharp contrast to the bulk counterpart which undergoes a semiconductor to semimetal transition under ~ 1.8 GPa, the band gap of 2 L increases with increasing pressure until beyond 2 GPa. Meanwhile, for a sample with a given layer number, the pressure-induced shift also differs for transitions with different indices. Through the tight-binding model in conjunction with a Morse potential for the interlayer coupling, this layer- and transition-index-dependent pressure effect can be fully accounted. Our study paves a way for versatile van der Waals engineering of two-dimensional BP.

DOI: 10.1103/PhysRevLett.127.186401

Recently, the renaissance of black phosphorus (BP) as an emerging layered two-dimensional (2D) semiconductor has attracted tremendous research interest [1–3]. Different from graphene and transition metal dichalcogenides, BP has a direct band gap ranging from 0.35 eV (bulk) to 1.7 eV (monolayer) [4,5], which, in conjunction with the remarkable in-plane anisotropy, makes BP a promising candidate for versatile optoelectronic devices [6–10].

Pressure can readily induce changes of lattice constants, especially the interlayer distance in layered 2D materials, hence modify the electronic properties of materials [11], such as semiconductor to metal transitions [12,13], band gap opening in gapless few-layer graphene [14], and band structure engineering in van der Waals heterostructures [15] and Moire superlattices [16,17]. Previous studies show that pressure induces a semiconductor-to-metal transition at ~ 1.8 GPa on bulk BP [18–20], which suggests that the band gap shrinks with increasing pressure. It is tempting to infer that even for thin layers, the band gap also shrinks under pressure and eventually closes up to become a metal [21]. However, except for a few studies on pressureinduced lattice structure transition in thin layers [22-24], there is no experimental report on the electronic structure to date.

Here, we systematically investigate the pressure effect on band structures of atomically thin BP (2–13 layers) through Fourier transform infrared spectroscopy. To our surprise, the pressure effect exhibits strong layer dependence, which strongly deviates from the bulk counterpart. For instance, with the pressure increasing to 2 GPa, the band gap of 2 L BP is enlarged rather than shrinking, while the band gap of the bulk is already closed at such pressure. Besides, due to the interlayer interaction, there are multiple optical resonances in few-layer BP, and pressure effect on these optical resonances also varies systematically. Through a tightbinding model in conjunction with a Morse potential, the quantitative evolution of the interlayer overlapping integrals is captured, and the physical mechanism responsible for the layer-dependent pressure effect is unveiled. Our work highlights the critical role played by the tunable interlayer coupling in van der Waals materials.

In our study, few-layer BP was mechanically exfoliated from the bulk crystal onto polydimethylsiloxane, then was transferred onto the diamond surface of a diamond anvil cell (DAC), as shown in Fig. 1(a). The layer number and crystal orientation were identified through infrared (IR) extinction spectrum [4,5]. The applied pressure was monitored by the shift of the photoluminescence peak of a ruby ball placed in the cell. To avoid degradation of few-layer BP, silicone oil was chosen as an inert pressure transmitting medium (PTM). (For details on the experiment procedure, see Methods in Supplemental Materials [25].) It should be noted that PTM usually plays a critical role in pressure experiments on 2D materials. It could compromise the reproducibility of experimental results [29] if the PTM is not optimized. While in our study, the pressure is limited in



FIG. 1. Pressure effect on electronic structures of few-layer BP. (a) Schematic illustration of the experimental setup for band structure engineering in few-layer BP through diamond anvil cell (DAC). (b) Optical image of a BP flake which contains 3 and 6 L in DAC. The region inside the red box is where the IR light shines. Scale bar is $20 \ \mu m$. (c) Schematic illustration of optical transitions between different subbands in bilayer BP. (d) Infrared extinction spectra of sample shown in Fig. 1(b) under different pressure. The spectra are offset vertically for clarity. (e) Peak position versus pressure for E_{11} of 3 L, E_{11} and E_{22} of 6 L, and band gap of a bulk BP from top to bottom, respectively. Dashed lines are a guide to the eye.

a moderate range (<4 GPa), the frequently used PTM is well hydrostatic [30], hence the PTM will not affect our results much and we can treat it as an ideal media.

Figure 1(b) is the photograph of a thin BP flake in the DAC, containing 3 and 6 L. Figure 1(d) shows infrared extinction spectra of this sample under different pressures ranging from 0 GPa (ambient pressure) to 3.22 GPa (the spectra are offset vertically for clarity). Three main peaks can be clearly identified [see Fig. 1(d)], which result from the exciton absorption of 3 and 6 L BP, labeled as E_{11} (the exciton associated with the first valance band to the first conduction band transition, namely the optical band gap [see Fig. 1(c)] and E_{22} (the second valance band to the second conduction band). The single particle band gap has a higher energy than the exciton peak position, with a separation as the exciton binding energy [31,32]. Since the pressure effect on single particle band gap plays a major role when the pressure is only moderate [33], for simplicity, we neglect the possible change of the exciton binding energy and attribute the band effect to the shift of the exciton peak position. Figure 1(e) plots the peak positions of E_{11} of 3 L, 6 L, E_{22} of 6 L, and the band gap of bulk BP versus pressure. As we can see, with increasing pressure, the E_{11} of 3 L exhibits a nonmonotonic shift, which undergoes redshift from the beginning and then blueshift for pressure above ~0.6 GPa, in stark contrast to the shift of the band gap in bulk BP [lower panel of Fig. 1(e)]. Meanwhile, E_{11} of 6 L shows a contrasted behavior as well, exhibiting a nonlinear redshift below ~1 GPa and then almost no shift from 1 to 2.92 GPa. The different shift of E_{11} in 3 and 6 L indicates the pressure effect on the band gap is strongly layer dependent. Besides, the pressureinduced shift of E_{22} in 6 L is dramatically different from E_{11} as well, exhibiting almost no change below 1 GPa but a blueshift above 1 GPa.

This transition-index dependence of the pressure effect is further verified in an 11 L BP shown in Fig. 2(a), where three optical resonances (E_{11} , E_{22} , E_{33}) can be observed. As shown in Fig. 2(b), E_{11} undergoes redshift nonlinearly with increasing pressure until it fully enters the silicone oil absorption region for pressure above ~1 GPa. In contrast, E_{33} first redshifts below ~0.5 GPa and then blueshifts above ~0.5 GPa, very similar to E_{11} of 3 L.



FIG. 2. Pressure effect on electronic structures of 11 L BP. (a) Infrared extinction spectra of a 11 L BP under different pressure. Silicone oil has strong absorption between 0.35 to 0.37 eV (shaded region). The spectra are offset vertically for clarity. (b) Peak position versus pressure for E_{11} , E_{22} , and E_{33} of 11 L.



FIG. 3. Pressure effect on the interlayer interaction of few-layer BP. (a) Schematic illustration for the evolution of the atomic structure of trilayer BP with pressure. (b) The relative changes of γ versus pressure. Dots are data extracted from E_{22} - E_{11} of 6 L, 7 L, 9 L, and E_{33} - E_{22} of 11 L. The solid curve is the fitting based on Eq. (3).

The pressure-induced shift of E_{22} is in-between E_{11} and E_{33} , which redshifts nonlinearly below 1 GPa and then slightly blueshifts, close to the behavior of E_{11} for the 6 L. In fact, this layer- and transition-index-dependent pressure effect is systematic. Figure S2 shows more data with different layer number ranging from 2 to 13. Besides the pressure-induced peak position shift, E_{11} (also E_{22}) of 6 L is barely discernable under 3.22 GPa, as shown in Fig. 1(d), which could result from the direct to indirect band gap transition [33,34]. However, E_{11} of 3 L is still discernible under this pressure, implying pressure-induced direct to indirect band gap transition also exhibits strong layer dependence, which deserves further investigation. In this study, we mainly investigate the pressure effect on the electronic structure in the direct band gap regime. Bearing in mind larger error bars for extraction of the peak position in higher pressure (especially higher than 2.5 GPa), we only focus on the pressure below 2.5 GPa in the following analysis.

Now we can take a closer look at the mechanism responsible for this layer- and transition-index dependence of the pressure effect. As mentioned earlier, multiple optical resonances in the same few-layer BP are due to the interlayer coupling. The energy separation of them is proportional to the interlayer coupling [35], which can offer us an unambiguous signature to monitor such coupling under pressure. According to previous studies [4,5], the transition energy of optical resonances in *N*-layer BP can be well described through the tight-binding model:

$$E_{nn}^{N}(P) = E_{g0}(P) - \gamma(P) \cos\left(\frac{n\pi}{N+1}\right), \qquad (1)$$

where $E_{g0}(P)$ is the monolayer band gap at pressure *P*, *n* is the subband index, $\gamma(P)$ is the difference of overlapping integrals for conduction band (γ_c), and valence band (γ_v), which is proportional to the interlayer hopping parameter (t^{\perp}) [35]. From Eq. (1), $\gamma(P)$ can be easily extracted through monitoring the peak separation between optical resonances in the same layer N but with different subband indices (n and m) with the following equation:

$$\gamma(P) = [E_{nn}^{N}(P) - E_{mm}^{N}(P)] / \left[\cos\left(\frac{m\pi}{N+1}\right) - \cos\left(\frac{n\pi}{N+1}\right) \right].$$
(2)

Figure 3(b) plots the relative change of γ , i.e., $\Delta \gamma = \gamma(P) - \gamma(0)$, versus P, extracted from $E_{22}-E_{11}$ of 6, 7, 9 L and E_{33} - E_{22} of 11 L. The enhancement of γ with increasing pressure is unambiguous in spite of the error bar. This is consistent with the expectation, since pressure can decrease the interlayer distance d [as shown in Fig. 3(a)]. As we can see in Fig. 3(b), the relative change of γ can be as large as 0.32 ± 0.08 eV under 1.92 GPa, corresponding to a remarkable change of $(18 \pm 4)\%$ [$\gamma(0)$ is 1.76 eV under ambient pressure [5]]. According to our previous studies, only $\sim 5\%$ change of interlayer interaction was achieved by biaxial in-plane strain or thermal expansion [36,37]. Apparently, compared to those tuning schemes, pressure is the most efficient way to tune the interlayer interaction in BP. It should be noted that $\gamma(P)$ extracted from samples with different layer number shows little difference with current error bars, suggesting thickness-independent layer distance under pressure. Hence, for simplicity, we assume no layer dependence for $\gamma(P)$ in the subsequent analysis.

More quantitatively, we can make use of Morse potential which is typically employed to model interatomic forces in molecules and is also applied for the interlayer interaction in transition metal dichalcogenides, as reported in recent studies [38]. Morse potential is written as $U(d) = U_{depth} \{1 - \exp[-(d - d_{eq})/d_{width}]\}^2$, where U_{depth} is the depth of the potential, d_{eq} is the equilibrium distance (here it can be regarded as the interlayer distance without external pressure), and d_{width} is the width of the potential. Through $P(d) = -\partial U/S\partial d$, where S is the basal area of BP, the pressure as a function of interlayer distance *d* can be obtained (see Supplemental Material [25]). Now let us revisit γ , which is mainly determined by the interlayer hopping parameter t^{\perp} [see Fig. 3(a)]. Generally, the hopping parameter is scaled as d^{-2} [39]. However, other models are adopted as well. Previous studies reveal that the interlayer hopping parameter can exhibit an exponential decay with *d* in bilayer graphene [40]. Here, we also take the exponential form for γ , i.e., $\gamma(d) = \gamma_0 e^{-(d-d_{eq})/d_0}$, where γ_0 is γ under 0 GPa and d_0 is a characteristic length. Without loss of generality and for simplicity, we assume that d_0 is equal to d_{width} , as has been done in Ref. [38]. Then the relationship between γ and *P* reads

$$\gamma(P) = \frac{\gamma_0}{2} \left(1 + \sqrt{1 + \frac{p}{p_{\rm coh}}} \right), \tag{3}$$

where $P_{\rm coh}$ is termed as cohesive pressure, representing the threshold pressure to be overcome in mechanical exfoliation of BP layers (details in Supplemental Material [25]). Since γ_0 is known, here only $P_{\rm coh}$ is to be determined. We use Eq. (3) to globally fit $\Delta \gamma$ shown in Fig. 3(b). The overall trend of the model fits well with the experiment data, and $P_{\rm coh}$ is obtained as 2.4 ± 1 GPa, comparable to those obtained in TMDCs [38].

With the obtained relation between the interlayer coupling and the pressure, the pressure effect on intralayer bonds can be accounted as well. According to previous studies [35], due to the absence of the interlayer coupling, monolayer band gap is mainly determined by two hopping parameters labeled as t_1^{\parallel} and t_2^{\parallel} [see Fig. 3(a)]. Besides, our previous studies have shown that the thin BP flake obtained through dry transferring is in good contact with the substrate [36,37]. Moreover, giving the small cross section on the side of a thin BP (noting the force F = PS, with S as the side area), it is reasonable to assume that when pressure is not large (as in our case), the thin BP flake always sticks tightly to the diamond surface and the in-plane lattice constants stay the same (the diamond surface has almost no deformation). This is also consistent with the scenario of graphene and quantum wells supported on substrates under pressure [41,42]. Based on this assumption, we know the pressure effect on E_{d0} is mainly due to the change of t_2^{\parallel} , since the corresponding bond is out of plane, as shown in Fig. 3(a). More specifically, with an increasing pressure, the monolayer thickness D [see Fig. 3(a)] decreases. As a result, t_2^{\parallel} is strengthened to induce an increase in E_{a0} . This is consistent with theoretical calculations of monolayer BP under normal strain [33,43]. To quantify E_{a0} dependence on P, we can make use of Morse potential as well. It should be noted that there is a covalence bond between atoms connected by t_2^{\parallel} , and the coupling between them is much stronger than the interlayer coupling, suggesting a larger $P_{\rm coh}$. When $P \ll P_{\rm coh}$, as in our case, E_{a0} will change linearly with P [refer to Eq. (3)] as follows:

$$\Delta E_{a0}(P) = aP, \qquad (4)$$

where $\Delta E_{a0}(P)$ is the relative change of E_{a0} , a is the changing rate, which is presumably positive. According to the x-ray diffraction study of few-layer BP [44], the pressure-induced change of the lattice constant along out-of-plane (D+d) shows no difference in different thickness BP. Moreover, as mentioned above, the change of the interlayer distance (d) also shows no layer dependence. Hence, it is reasonable to assume that the pressureinduced change of the intralayer height (D) has no layer dependence as well, suggesting a in Eq. (4) is the same for different thickness BP. Based on these assumptions, we can gain some interesting insights. For example, the pressureinduced shift in E_{11} of 3 L, E_{22} of 7 L, and E_{33} of 11 L should be the same, since $\cos[n\pi/(N+1)]$ is the same in these optical transitions [see Eq. (1)]. Indeed, this is what we have observed in Fig. S3, which further validates our assumptions.

Finally, combining Eqs. (1), (3), and (4), the pressureinduced shift of the band gap can be written as

$$\Delta E_{11}^{N}(P) = aP - \frac{\gamma_0}{2} \left(\sqrt{1 + \frac{p}{p_{\rm coh}}} - 1 \right) \, \cos\left(\frac{1}{N+1}\pi\right),\tag{5}$$

which reproduces the experimental results for samples with different thickness up to 50 nm, as shown in Fig. 4. The overall trend of fitting curves agrees well with the experiment data. A global fitting procedure, which excludes the bulk data in Fig. 4 (reasons will be discussed later), gives *a* of 0.18 ± 0.03 eV/GPa, corresponding to ~1% normal strain on monolayer under 1 GPa [43]. Moreover, *P*_{coh} is 1.4 ± 0.1 GPa, which is consistent with the one extracted from $\Delta\gamma$ in Fig. 3(b) within the error bar. Beside the band



FIG. 4. The relative change of optical band gaps of BP versus pressure. Dots are experiment data and solid curves are the fitting curves. The thickness of the thin film and bulk shown in the figure are \sim 50 nm and 1 μ m, respectively.

gap, the pressure-induced shift of optical resonances with higher transition indices (E_{22}, E_{33}) can be reproduced as well (shown in Fig. S4 [25]). At last, we can clearly see this layer- and transition-index-dependent pressure effect is due to the change of the interlayer interaction $\Delta \gamma$.

To globally fit the data in Fig. 4 with Eq. (5), there is a basic assumption that samples with different thickness have the same lattice constants under a given pressure. Intuitively, this can be satisfied for few-layer and thin films, since they can stick to the diamond surface equally well. However, for even thicker samples, like the bulk one with thickness of $1 \mu m$ in Fig. 4, the force induced by the pressure from the side of the flake can be large enough to loose the contact to the diamond surface and the overall pressure effect turns to be truly hydrostatic. In other words, besides the normal strain, there is additional in-plane compressive strain in the bulk BP. As demonstrated previously, such strain also shrinks the band gap [36]. Therefore, the band gap of the bulk under hydrostatic pressure decreases faster than the one under normal strain. This explains the dramatic deviation of the bulk sample from others in Fig. 4, even though the band gap of the bulk is almost the same as the 50 nm thick film if they are under the same condition (e.g., at ambient pressure), as shown in the IR extinction spectrum (see Fig. S5 [25]). The band gap of the bulk redshifts linearly with pressure (shift rate is 0.19 eV/GPa, see Fig. 4), and is ultimately closed at \sim 1.8 GPa, which is fully consistent with previous studies in bulk BP with truly hydrostatic pressure [18]. The different conditions of the bulk and thin film under pressure were further verified by monitoring the phonon frequency through Raman spectroscopy (see Fig. S5 [25]). If we regard the bulk sample is under hydrostatic pressure, fewlayer and thin films of BP experience nonhydrostatic one, which is more like a uniaxial strain normal to the 2D plane. The substrate plays a very important role and tightly holds the few-layer BP along in-plane directions.

In summary, we have systematically investigated the layer-dependent pressure effect on electronic structures of 2D BP. Through the tight-binding model in conjunction with a Morse potential, we have quantified the evolution of the band gap with pressure, and unveiled that the layerdependent pressure effect on electronic structures of 2D BP is mainly due to the pressure-induced enhancement of the interlayer coupling. Future studies can be devoted to the possible layer-dependent semiconductor-to-metal transition under higher pressure.

H. Y. is grateful to the National Key Research and Development Program of China for financial support (Grants No. 2017YFA0303504 and No. 2016YFA0203900), the National Natural Science Foundation of China (Grants No. 11874009, No. 12074085, No. 11734007), the Natural Science Foundation of Shanghai (Grant No. 20JC1414601) and the Strategic Priority Research Program of Chinese Academy of Sciences (XDB30000000). S. H. acknowledges China Postdoctoral Science Foundation (Grant No. 2020TQ0078). G. Z. acknowledges the financial support from the National Natural Science Foundation of China (Grant No. 11804398), Natural Science Basic Research Program of Shaanxi (Grant No. 2020JQ-105), and the Joint Research Funds of Department of Science & Technology of Shaanxi Province and Northwestern Polytechnical University (Grant No. 2020GXLH-Z-026). This work was partially supported by the National Natural Science Foundation of China (Grants No. 42050203, No. U1530402 and No. U1930401). Y. Lu thank Dr. L.P. Kong of HPSTAR and the staffs from BL01B beamline of National Facility for Protein Science in Shanghai (NFPS) at Shanghai Synchrotron Radiation Facility (SSRF), for assistance with the preliminary HP-IR experiments. Partial experimental research used the resources of SSRF (BL15U1 and BL06B) and the Advanced Light Source (ALS, Beamline 1.4.3), which is a DOE Office of Science User Facility under contract No. DE-AC02-05CH11231.

^{*}These authors contributed equally to this work. [†]yang.lu@hpstar.ac.cn [‡]hgyan@fudan.edu.cn

- [1] L. Li, Y. Yu, G. J. Ye, Q. Ge, X. Ou, H. Wu, D. Feng, X. H. Chen, and Y. Zhang, Nat. Nanotechnol. 9, 372 (2014).
- [2] X. Ling, H. Wang, S. Huang, F. Xia, and M. S. Dresselhaus, Proc. Natl. Acad. Sci. U.S.A. 112, 4523 (2015).
- [3] A. Castellanos-Gomez, J. Phys. Chem. Lett. 6, 4280 (2015).
- [4] L. Li et al., Nat. Nanotechnol. 12, 21 (2017).
- [5] G. Zhang, S. Huang, A. Chaves, C. Song, V. O. Ozcelik, T. Low, and H. Yan, Nat. Commun. 8, 14071 (2017).
- [6] H. Yuan et al., Nat. Nanotechnol. 10, 707 (2015).
- [7] M. C. Sherrott, W. S. Whitney, D. Jariwala, S. Biswas, C. M. Went, J. Wong, G. R. Rossman, and H. A. Atwater, Nano Lett. 19, 269 (2019).
- [8] C. Chen et al., Sci. Adv. 6, eaay6134 (2020).
- [9] Y. Zhang et al., Adv. Mater. 32, e1808319 (2020).
- [10] J. Wang, A. Rousseau, M. Yang, T. Low, S. Francoeur, and S. Kena-Cohen, Nano Lett. 20, 3651 (2020).
- [11] L. Zhang et al., Adv. Sci. (Weinh) 7, 2002697 (2020).
- [12] Z. Zhao et al., Nat. Commun. 6, 7312 (2015).
- [13] A. P. Nayak et al., Nat. Commun. 5, 3731 (2014).
- [14] F. Ke et al., Proc. Natl. Acad. Sci. U.S.A. 116, 9186 (2019).
- [15] J. Xia et al., Nat. Phys. 17, 92 (2021).
- [16] M. Yankowitz et al., Nature (London) 557, 404 (2018).
- [17] Y. Gao, X. Lin, T. Smart, P. Ci, K. Watanabe, T. Taniguchi, R. Jeanloz, J. Ni, and J. Wu, Phys. Rev. Lett. **125**, 226403 (2020).
- [18] Y. Akahama and H. Kawamura, Phys. Status Solidi B 223, 349 (2001).
- [19] Z. J. Xiang et al., Phys. Rev. Lett. 115, 186403 (2015).
- [20] X. Li et al., Proc. Natl. Acad. Sci. U.S.A. 116, 1065 (2019).
- [21] P.-L. Gong, B. Deng, L.-F. Huang, L. Hu, W.-C. Wang, D.-Y. Liu, X.-Q. Shi, Z. Zeng, and L.-J. Zou, J. Phys. Chem. C 121, 20931 (2017).
- [22] G. Xiao et al., Nanoscale 9, 10741 (2017).
- [23] T. Sasaki, K. Kondo, Y. Akahama, S. Nakano, and T. Taniguchi, Jpn. J. Appl. Phys. 56, 05FB06 (2017).

- [24] A. Kundu, D. Tristant, N. Sheremetyeva, A. Yoshimura, A. Torres Dias, K. S. Hazra, V. Meunier, and P. Puech, Nano Lett. 20, 5929 (2020).
- [25] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.127.186401 for details of methods, stability of BP in DAC, additional data of pressure effect on BP, quantifying interlayer coupling with pressure, which includes Refs. [26–28].
- [26] A. Castellanos-Gomez, M. Buscema, R. Molenaar, V. Singh, L. Janssen, H. S. J. van der Zant, and G. A. Steele, 2D Mater. 1, 011002 (2014).
- [27] H. K. Mao, J. Xu, and P. M. Bell, J. Geophys. Res. 91, 4673 (1986).
- [28] F. Wang, G. Zhang, S. Huang, C. Song, C. Wang, Q. Xing, Y. Lei, and H. Yan, Phys. Rev. B 99, 075427 (2019).
- [29] P. Shen, Q. Li, H. Zhang, R. Liu, B. Liu, X. Yang, Q. Dong, T. Cui, and B. Liu, Phys. Status Solidi (b) 254, 1600798 (2017).
- [30] S. Klotz, J. C. Chervin, P. Munsch, and G. Le Marchand, J. Phys. D 42, 075413 (2009).
- [31] A. Chernikov, T. C. Berkelbach, H. M. Hill, A. Rigosi, Y. L. Li, O. B. Aslan, D. R. Reichman, M. S. Hybertsen, and T. F. Heinz, Phys. Rev. Lett. **113**, 076802 (2014).
- [32] G. W. Zhang, A. Chaves, S. Y. Huang, F. J. Wang, Q. X. Xing, T. Low, and H. G. Yan, Sci. Adv. 4, eaap9977 (2018).

- [33] L. Seixas, A. S. Rodin, A. Carvalho, and A. H. Castro Neto, Phys. Rev. B **91**, 115437 (2015).
- [34] A. Manjanath, A. Samanta, T. Pandey, and A. K. Singh, Nanotechnology 26, 075701 (2015).
- [35] A. N. Rudenko and M. I. Katsnelson, Phys. Rev. B 89, 201408(R) (2014).
- [36] S. Huang, G. Zhang, F. Fan, C. Song, F. Wang, Q. Xing, C. Wang, H. Wu, and H. Yan, Nat. Commun. 10, 2447 (2019).
- [37] S. Huang et al., Phys. Rev. Lett. 125, 156802 (2020).
- [38] P. Ci et al., Nano Lett. 17, 4982 (2017).
- [39] S. Yongke, T. Sccot E, and N. Toshikazu, *Strain Effect in Semiconductors Theory and Device Applications* (Springer, New York, 2010).
- [40] G. Trambly de Laissardière, D. Mayou, and L. Magaud, Nano Lett. 10, 804 (2010).
- [41] C. Bousige et al., Nano Lett. 17, 21 (2017).
- [42] J. Wu, W. Walukiewicz, K. M. Yu, J. W. Ager, E. E. Haller, H. Lu, W. J. Schaff, Y. Saito, and Y. Nanishi, Appl. Phys. Lett. 80, 3967 (2002).
- [43] H. J. Duan, M. Yang, and R. Q. Wang, Physica (Amsterdam) 81E, 177 (2016).
- [44] Q. Li, H. Huang, Z. Chen, X. Huang, K. Deng, S. Luo, Z. Wang, X. Yu, and Z. Quan, Adv. Electron. Mater. 5, 1800712 (2019).